Global plasma simulation of charge state distribution inside a 2.45 GHz ECR plasma with experimental verification

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Abstract

For the first time, the charge state distribution inside the MEsskammer für FlugzeitInStrumente und Time-Of-Flight (MEFISTO) electron cyclotron resonance (ECR) plasma and in the extracted ion beam was successfully simulated. A self-consistent ECR plasma ionization model (Hohl M 2002 MEFISTO II: Design, setup, characterization and operation of an improved calibration facility for solar plasma instrumentation PhD Thesis University of Bern) was further developed, recomputing the ion confinement time for every ion species and in every time step based on the actual plasma potential rather than using a prescribed constant ion confinement time. The simulation starts with a user defined set of initial conditions and develops the problem in time space by an adaptive step length fourth order Runge–Kutta (RK4) solver, considering particle densities based on ionization rates, recombination rates, ion confinement times and plasma potential. At the simulation end, a steady-state ion charge state distribution is reached, which is in excellent agreement with the measured ion beam charge state distribution of the MEFISTO ion source for Ar⁺ to Ar⁵⁺ and in good agreement for Ar⁶⁺.

(Some figures in this article are in colour only in the electronic version)

1. Introduction

The development of advanced permanent magnetic materials, able to supply magnetic fields for ECR frequencies of 10 GHz and more [4], makes the application of solenoids for plasma confinement in ECR ion sources obsolete in many new developed high voltage particle accelerators. The charge state distribution of an ion source critically depends on its design parameters, especially the magnetic confinement field and the excitation frequency. Consequently, the choice of a permanent magnetic confinement asks for a precise planning and design [3] before the production process due to very limited possibilities of field manipulation after the production of the magnetic confinement system. This paper presents a numerical simulation of the argon charge state distribution before production, thereby significantly improving a successful ion source realization with the desired charge state distribution.

In this paper we present the plasma simulation in section 2 and its simulation results in section 3. In section 4 we discuss the simulation results, followed by our conclusion in section 5.

2. The plasma simulation

First, the existing plasma model by Hohl et al [5] is presented in section 2.1, followed by modifications to the model in section 2.2 and the numerical implementation in section 2.3.

2.1. The existing plasma model

The concept of a self-consistent ECR plasma model [5] was used to develop the presented numerical simulation. The plasma model aims at keeping the free parameters as low as possible to ensure simplicity and reliability compared with earlier, more sophisticated and more complex plasma models
The model concept is based on particle density balance (equation (1)):

\[ \frac{dN_j}{dt} = \text{source-sink-loss} \]  

(1)

with \( N_j \) denoting the respective particle density of charge state \( j \), neutrals and electrons. The plasma model considers ionization and recombination rates, IR and RR, respectively, using two electron populations at two fixed temperatures, for the cold and the hot electron population [2]. The reaction rates [16, 17] are linearly combined using a fixed fraction of hot electrons \( f_{\text{h/e}} \) (equations (2) and (3)):

\[ IR_{j-1,j} = f_{\text{h/e}} \cdot IR_{j-1,j}^{\text{hot}} + (1 - f_{\text{h/e}}) \cdot IR_{j-1,j}^{\text{cold}} \]  

(2)

\[ RR_{j+1,j} = f_{\text{h/e}} \cdot RR_{j+1,j}^{\text{hot}} + (1 - f_{\text{h/e}}) \cdot RR_{j+1,j}^{\text{cold}} \]  

(3)

where \( f_{\text{h/e}} \) is the fraction of hot electrons present in the ECR plasma, \( IR_{j-1,j}^{\text{hot}} \) is the ionization rate for the hot electrons, \( RR_{j+1,j}^{\text{hot}} \) is the ionization rate for the cold electrons. \( f_{\text{h/e}} \) is a free parameter, i.e. it is not derived from the model but can be chosen by the user based on experimental evidence for the free parameter, i.e. it is not derived from the model but can be chosen by the user based on experimental evidence for the ion confinement times (in the range 1–30%).

Ionization is known to be a step-by-step process [2, 5] where double ionization from \( \text{Ion}^{j+} \) to \( \text{Ion}^{(j+2)+} \) can be neglected and single ionization from \( \text{Ion}^{j+} \) to \( \text{Ion}^{(j+1)+} \) is the dominant process. A neutral balance equation (equation (4)) and an ion balance equation array (equations (4)–(8)) are used to compute the time derivative for the fourth order Runge–Kutta (RK4) algorithm. The neutral gas density in the ion source is kept constant by the gas pressure regulation.

\[ \frac{dn_{\text{gas}}(t)}{dt} = 0, \]  

(4)

\[ \frac{dn_1(t)}{dt} = n_e(t) \cdot [n_{\text{gas}}(t) \cdot IR_{0,1} + n_2(t) \cdot RR_{2,1} - n_1(t) \cdot IR_{1,2} - n_1(t) \cdot RR_{1,0}] \]  

(5)

\[ \vdots \]

\[ \frac{dn_j(t)}{dt} = n_e(t) \cdot [n_{j-1}(t) \cdot IR_{j-1,j} + n_{j+1}(t) \cdot RR_{j+1,j} - n_j(t) \cdot IR_{j,j+1} - n_j(t) \cdot RR_{j,j-1}] \]  

(6)

\[ \vdots \]

\[ \frac{dn_{\text{max}}(t)}{dt} = n_e(t) \cdot \left[ n_{\text{max}-1}(t) \cdot IR_{\text{max}-1,\text{max}} - n_{\text{max}}(t) \right] \cdot RR_{\text{max}-1,\text{max}} \]  

(7)

\[ \frac{dn_e(t)}{dt} = n_e(t) \cdot \left[ n_{\text{gas}} \cdot IR_{0,1} \sum_{j=1}^{\text{max}-1} n_j(t) \cdot IR_{j,j+1}^\text{max} - \sum_{j=1}^{\text{max}} n_j(t) \cdot RR_{j,j-1} \right] - \frac{n_e(t)^{3/2}}{a \cdot \epsilon_e}, \]  

(8)

where \( n_{\text{gas}} \) is the neutral gas density, \( n_j \) is the ion density of charge state \( j \), \( IR_{j-1,j} \) is the ionization rate from charge state \( j - 1 \) to charge state \( j \). The recombination rate from charge state \( j + 1 \) to charge state \( j \) and \( \tau_{\text{ion},j} \) is the mean ion confinement time. A similar balance equation is used [5] for the electron population (equation (9)).

### 2.2. Modifications to the existing plasma model

In the plasma model of Hohl et al 2002 [5], all particle confinement times \( \tau_{\text{ion},j} \) and \( \tau_e \) are fixed. This allows a computationally economic implementation and it gives direct control over these parameters. However, due to fixed confinement times, the model is not able to simulate loss or keeping of particles depending on the actual plasma state and quasi-neutrality is not ensured, leading to a plasma potential which does not agree with theory or measurements. The modified plasma model makes use of combined magnetic and electrostatic confinement times for ions, updated in every computation step.

The magnetic confinement is provided by the permanent magnetic setup, which also provides the ECR field.

In addition, hot ECR electrons feature a strong anisotropic velocity distribution with preference perpendicular to the local magnetic field direction [1] resulting from the ECR heating process. This leads to a negligible loss cone fraction and a very good confinement before the respective hot electrons are lost due to scattering or ionization. Cold electrons are supposed to feature an isotropic velocity distribution equal to one of the ions. At the same kinetic energy and local magnetic field, electrons have a smaller Larmor radius than ions, which improves cold electron confinement compared with the ion confinement. All this leads to a slightly negative plasma potential [4, 10, 11], experimentally verified by Golovanivsky and Melin in 1992 [7]. The negative plasma potential ensures a proper confinement of the ions, long enough for step-by-step ionization up to high charge states.

The actually used ion confinement time is calculated by equation (10), according to Geller [2] and modified by \( a \) an additional parameter to allow linear modification of the ion confinement time (see section 4).

\[ \tau_{\text{ion},j} = r_m \cdot L_m \cdot a \cdot \sqrt{\frac{\pi}{2}} \cdot m_i \cdot \exp \left( \frac{j \cdot \Phi}{T_i} \right). \]  

(10)

Here, \( r_m \) is the magnetic mirror ratio, \( L_m \) the mirror length given by its two maxima, \( m_i \) the ion mass, \( T_i \) the ion temperature, \( j \) the charge state of the respective ion species and \( \Phi \) is the plasma potential. The bulk of the electrons is represented by cold electrons [2]. Their kinetic energy distribution and their scattering pattern with respect to the local magnetic field can be assumed to be isotropic. Since the geometric extent of the ECR plasma is much larger (plasma diameter: 26 mm) than the plasma Debye length (34 \( \mu \)m), we can assume quasi-neutrality and a homogeneous charge state distribution inside the approximately spherical ECR plasma. Then we can calculate the plasma potential by equation (11):

\[ \Phi = \frac{\rho \cdot r_m^2}{6e_0}. \]  

(11)
Table 1. Summary of initial conditions and simulation parameters for the plots shown in figures 1 and 2.

<table>
<thead>
<tr>
<th>Initial conditions</th>
<th>Value</th>
<th>S</th>
</tr>
</thead>
<tbody>
<tr>
<td>Electron density</td>
<td>100 (cm⁻³)</td>
<td>u</td>
</tr>
<tr>
<td>Ion density</td>
<td>0 (cm⁻³)</td>
<td>u</td>
</tr>
<tr>
<td>Gas density</td>
<td>4.83 × 10¹⁰ (cm⁻³)</td>
<td>u</td>
</tr>
<tr>
<td>Mirror ratio</td>
<td>4.15</td>
<td>[5]</td>
</tr>
<tr>
<td>Argon ion mass</td>
<td>39.95 (amu)</td>
<td>u</td>
</tr>
<tr>
<td>Confinement time τₑ</td>
<td>160 (s)</td>
<td>u</td>
</tr>
<tr>
<td>Hot electron fraction</td>
<td>0.25</td>
<td>u</td>
</tr>
<tr>
<td>Hot electron temp.</td>
<td>1700 (eV)</td>
<td>[6]</td>
</tr>
<tr>
<td>Cold electron temp.</td>
<td>1.7 (eV)</td>
<td>[5]</td>
</tr>
<tr>
<td>Ion temperature</td>
<td>1.7 (eV)</td>
<td>[5]</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Simulation parameters</th>
<th>Value</th>
<th>S</th>
</tr>
</thead>
<tbody>
<tr>
<td>maxerror</td>
<td>10⁻⁸</td>
<td>u</td>
</tr>
<tr>
<td>Initial time step size</td>
<td>10⁻¹⁰ (s)</td>
<td>u</td>
</tr>
<tr>
<td>Ion conf. modifier a</td>
<td>2.0</td>
<td>u</td>
</tr>
</tbody>
</table>

Note: S—Source of parameter value, u—user defined.

with \( \rho \) as the total plasma charge density and \( r_{pl} \) the plasma radius.

By updating the plasma potential \( \Phi \) and the ion confinement time \( \tau_{ion,j} \) in every time step, this method effectively regulates charge imbalance in a realistic way. It directly affects the ion densities by lowering or increasing the respective ion confinement time based on the actual electron and ion densities. In contrast, the electron confinement time had to be fixed in order to enable a successful plasma density evolution, which is discussed below.

2.3. The numerical implementation

A fourth order Runge–Kutta method with adaptive step length was developed to solve the given set of equations (equations (5)–(9)). To optimize development time and computational performance Python was chosen as a programming language, using the Numpy extension for array handling.

The implemented adaptive step length algorithm uses a double step length result in every other iteration to compare with the result of the actual step length. The step length is decreased, if the relative difference between double and single step length result is larger than a user defined threshold maxerror, otherwise the step length is increased. A simulation run for \( \text{Ar}^{1+} \) to \( \text{Ar}^{8+} \) and maxerror = 10⁻⁸ takes 5 h on an Intel Core 2 Duo 2.8 GHz system with 2 GB of RAM using only one of the two available CPU cores and a Xubuntu 8.10 operating system.

3. Simulation results

To obtain a best fit to the measured ion charge state distribution of the MEFISTO ion beam, the used initial conditions and simulation parameters are given in table 1.

The two parameters \( f_{h/e} \) and the ion confinement time modifier \( a \) are connected and are based on experimental evidence. For a 2.45 GHz ECR ion source such as MEFISTO, \( f_{h/e} \) will not be above 0.5 due to the limited ionization states measured in the extracted ion beam. In order to keep \( f_{h/e} \) below 0.5, the ion confinement time modifier \( a = 2.0 \) is chosen. This allows us to use a value \( f_{h/e} = 0.25 \). Figure 1 shows the simulation result of the plasma state time evolution for the electron density, all simulated ion charge state densities and the plasma potential.

The resulting time evolution of the plasma state is continuous for all simulation parameters. The electron density and the density of every charge state is monotonically increasing and reach steady state before 0.1 s in agreement with the experimental observations. The time evolution of the plasma potential features a maximum at 0.01 s and declines to −0.41 V which is in agreement with the literature values [4, 7]. In addition, we observe an exponential growth of the higher argon charge states around 0.01 s, the time of maximum plasma potential. Table 2 gives a summary of the simulated steady-state plasma particle density and the plasma potential values. Table 3 gives the electron confinement time applied as a simulation parameter and the ion confinement times resulting from the magnetic mirror, the updated plasma potential and the ion confinement time modifier \( a = 2.0 \) at steady state.

The simulation delivers ad hoc the charge state distribution inside the ECR plasma. However, to verify the simulated ion charge state densities with a measured ion charge state distribution of the extracted ion beam of MEFISTO, the simulation result needs to be modified by an extraction function. Due to the charge-state-sensitive combined magnetic and electrostatic confinement of the ions (see equation (10)),
and currents are normalized to Ar1+.

measured extracted ion beam from MEFISTO. All densities plasma, the corrected extracted simulation ion beam and the between the simulated ion charge state distribution in the ECR T T transforms the plasma ion charge state distribution into the plasma charge density in elementary charges steady-state particle densities, the plasma potential, the combined due to the different charge-to-mass ratio. Equation (12) the plasma itself. Generally, low ion charge states can in the ion source to be significantly higher than the insides its ECR plasma, the corrected distribution for the extracted ion beam and the measured charge state distribution in the extracted ion beam of MEFISTO [5].

4. Discussion

The shortfall of the measured Ar7+ and Ar8+ ion currents in MEFISTO compared with the simulation result may be explained as follows. The simulation uses a simple and robust macroscopic plasma model including plasma potential time evolution. More complex or microscopic plasma phenomena are not considered such as geometry dependent oscillations, wave phenomena or higher order ionization mechanisms. Hence the expected, simple exponential regress of the simulated charge state distribution. In addition, the background particle density (i.e. the residual gas) in the beam transport system of MEFISTO causes charge exchange between the neutral gas molecules and the multiply charged ions, reducing their charge by one at each charge exchange event. The probability for this charge exchange rises non-linearly with the charge states and results in a preferential loss of higher charge states. This agrees with the slight surplus of Ar6+ in the measurement compared with the simulation. Furthermore, the parameters of the ion optics, facilitating the beam transport from the ion source to the ion current collector, can be optimized for a single charge state only. This penalizes other charge states.

In the literature [2], equation (10) without the additional ion confinement time modifier \( a \) is based on the assumption that an ion is experiencing about one bounce in the magnetic mirror on average before being lost through the mirror loss cone by scattering. To obtain a simulation result in good agreement with the measurement and to keep the hot electron fraction \( f_{he} \) as low as 0.25, an ion confinement time modifier \( a = 2.0 \) had to be chosen. Therefore, the parameter \( a \) can be interpreted as an ion experiencing two bounces on average in the magnetic mirror before being lost through the loss cone instead of being.
lost after only one bounce. Due to the approximative nature of the one-bounce theory, this slight modification is considered to be acceptable.

The resulting electron density does not exceed the cut-off density given by the MEFISTO microwave frequency. The electron density of the simulation result is therefore in excellent agreement with the literature [1, 2]. However, to obtain the presented electron density in the simulation in order to provide the necessary ionization basis and the plasma potential, an average electron confinement time of 160 s is required. The presented plasma model does not take into account secondary electrons emitted from the plasma chamber wall, nor does it distinguish between a cold and a hot electron population in the time evolution. In a modified simulation, in which the contribution of secondary electrons from walls to the plasma is considered, the electron confinement time of 160 s can be reduced by at least a factor of 10 to maintain the otherwise same simulation parameters and to obtain identical simulation results. The importance of secondary electrons for the ECR plasma has been recognized in several experiments [18–21].

To produce multi-charged ions with low atomic Z number, Geller [2] requires \( n_e/n_0 > 1 \), \( n_e \cdot \tau_i \sim 10^8 \) (s cm\(^{-3}\)) and \( T_{\text{cold}} < 100 \text{eV} \). For argon and a medium charge state of \( \text{Ar}^{+5} \), all these requirements are fulfilled by the results of our simulation.

A previous global ECR plasma model by Oda et al [8] use constant ion confinement times which are independent of the respective ion charge states. In our simulation, the ion confinement time is recomputed in every time step based on the actual plasma potential which, in turn, is also recomputed in every time step based on the actual electron density and the charge state distribution. In addition, Oda et al uses a different set of ion balance equations with additional sum terms, also considering direct ionization from neutrals to higher charge states as opposed to our model which uses single step ionization only (see section 2.1).

Another previous global ECR plasma model by Skalyga et al 2006 [9] simulates an opposing solenoid, pulsed and high power ECR plasma of a different kind. The resulting electron densities are three orders of magnitude higher than the one-bounce theory, this slight modification is considered to be acceptable.

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Furthermore, in this simulation a double bounce input parameter in the magnetic mirror of MEFISTO is necessary to confine the ions long enough to result in the measured charge state distribution and in order to limit the hot electron fraction as low as 0.25.

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References


